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**Título:** Zeta Functions For Two-Dimensional Shifts Of Finite Type

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**Sinopsis**

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This work is concerned with zeta functions of two-dimensional shifts of finite type. A two-dimensional zeta function  $\zeta_0(s)$ , which generalizes the Artin-Mazur zeta function, was given by Lind for  $\mathbb{Z}^2$ -action  $\sigma$ . In this paper, the  $n$ th-order zeta function  $\zeta_n$  of  $\sigma$  on  $\mathbb{Z}^{n \times 8}$ ,  $n=1$ , is studied first. The trace operator  $T_n$ , which is the transition matrix for  $x$ -periodic patterns with period  $n$  and height 2, is rotationally symmetric. The rotational symmetry of  $T_n$  induces the reduced trace operator  $t_n$  and  $\zeta_n = (\det(I - s t_n))^{-1}$ .

The zeta function  $\zeta_n = (\det(I - s t_n))^{-1}$  in the  $x$ -direction is now a reciprocal of an infinite product of polynomials. The zeta function can be presented in the  $y$ -direction and in the coordinates of any unimodular transformation in  $GL_2(\mathbb{Z})$ . Therefore, there exists a family of zeta functions that are meromorphic extensions of the same analytic function  $\zeta_0(s)$ . The natural boundary of zeta functions is studied. The Taylor series for these zeta functions at the origin are equal with integer coefficients, yielding a family of identities, which are of interest in number theory. The method applies to thermodynamic zeta functions for the Ising model with finite range interactions.

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