

Librería
Bonilla y Asociados
desde 1950



Título: Zeta Functions For Two-Dimensional Shifts Of Finite Type

Autor: Ban, Jung-Chao; Wen-Guei Hu; Song-Sun Lin;
Yin-Heng Lin

Precio: \$876.40

Editorial:

Año: 2013

Tema:

Edición: 1^a

Sinopsis

ISBN: 9780821872901

This work is concerned with zeta functions of two-dimensional shifts of finite type. A two-dimensional zeta function $\zeta_0(s)$, which generalizes the Artin-Mazur zeta function, was given by Lind for \mathbb{Z}^2 -action σ . In this paper, the n th-order zeta function ζ_n of σ on $\mathbb{Z}^{n \times 8}$, $n=1$, is studied first. The trace operator T_n , which is the transition matrix for x -periodic patterns with period n and height 2, is rotationally symmetric. The rotational symmetry of T_n induces the reduced trace operator t_n and $\zeta_n = (\det(I - s t_n))^{-1}$.

The zeta function $\zeta_n = \prod_{k=1}^{\infty} (\det(I - s t_n^k))^{-1}$ in the x -direction is now a reciprocal of an infinite product of polynomials. The zeta function can be presented in the y -direction and in the coordinates of any unimodular transformation in $GL_2(\mathbb{Z})$. Therefore, there exists a family of zeta functions that are meromorphic extensions of the same analytic function $\zeta_0(s)$. The natural boundary of zeta functions is studied. The Taylor series for these zeta functions at the origin are equal with integer coefficients, yielding a family of identities, which are of interest in number theory. The method applies to thermodynamic zeta functions for the Ising model with finite range interactions.

Table of Contents

- !Introduction
- !Periodic patterns
- !Rationality of ζ_n !More symbols on larger lattice
- !Zeta functions presented in skew coordinates
- !Analyticity and meromorphic extensions of zeta functions
- !Equations on \mathbb{Z}^2 with numbers in a finite field
- !Square lattice Ising model with finite range interaction
- !Bibliography